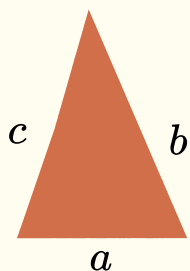


## Triangle

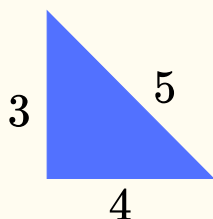
**Triangle Inequality:**

The sum of any two sides of a triangle is greater than the third side.

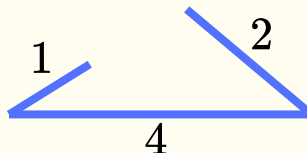
$$a + b > c, a + c > b, b + c > a$$

The difference of two sides is less than the third side.

$$c - a < b, c - b < a, b - c < a, b - a < c, a - b < c, a - c < b$$

**Example:**

$$3 + 4 > 5$$

**Example:**

$$1 + 2 \leq 4$$



If  $a \geq b \geq c > 0$ :  $b + c > a$   valid triangle.

★ For each group, determine whether the three side lengths can form a triangle.

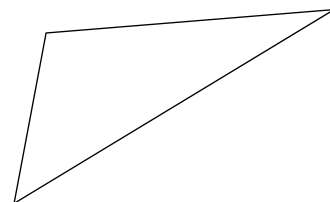
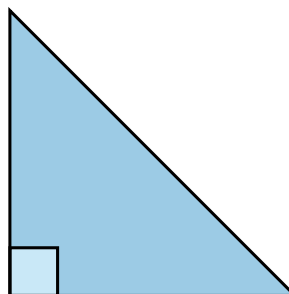
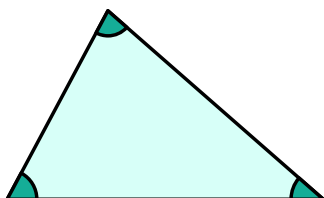
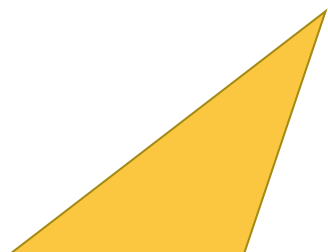
Group 1:  $a = 13, b = 14, c = 15$ (A) Yes (B) No 1:  $13+14 > 15$ , yesGroup 2:  $a = 2, b = 5, c = 2$ (A) Yes (B) No 2:  $2+2 < 4$ , noGroup 3:  $a = 8, b = 15, c = 7$ (A) Yes (B) No 3:  $7+8 = 15$ , noGroup 4:  $a = 0.6, b = 1.2, c = 1.5$ (A) Yes (B) No 4:  $0.6+1.2 > 1.5$ , yesGroup 5:  $a = \frac{1}{2}, b = \frac{1}{6}, c = \frac{1}{3}$ (A) Yes (B) No 5:  $\frac{1}{6} + \frac{1}{3} = \frac{1}{2}$ , no

★ In a triangle, two sides have lengths 32 and 47. Choose the possible length(s) of the third side from the options below: CDE

A. 10 B. 15 C. 23.5 D. 38 E. 62 F. 101

A. 10, 32, 47:  $10 + 32 = 42 \leq 47$ , noD. 32, 38, 47:  $32 + 38 = 70 > 47$ , yesB. 15, 32, 47:  $15 + 32 = 47 \leq 47$ , noE. 32, 47, 62:  $32 + 47 = 79 > 62$ , yesC. 23.5, 32, 47:  $23.5 + 32 = 55.5 > 47$ , yesF. 32, 47, 101:  $32 + 47 = 79 \leq 101$ , no

★ Match



Acute triangle

Right triangle

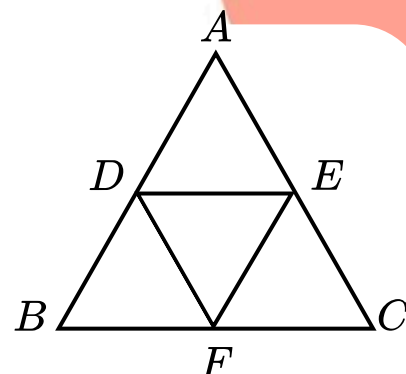
Obtuse triangle



## Triangle

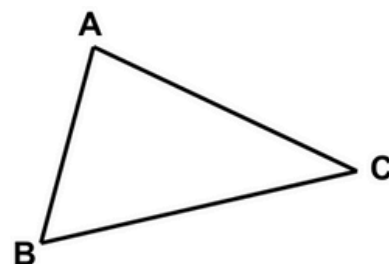
- ★  $\triangle ABC$  is equilateral. Points D, E, and F are the midpoints of sides AB, AC, and BC, respectively. There are 5 equilateral triangles in the figure in total.

$\triangle ABC$   
 $\triangle ADE$   
 $\triangle BDF$   
 $\triangle CEF$   
 $\triangle DEF$



- ★ Given that  $m\angle A = 86^\circ$  and  $m\angle C = 39^\circ$ ,  $m\angle B =$  55  $^\circ$ .

$$\begin{aligned}
 m\angle B &= 180^\circ - m\angle A - m\angle C \\
 &= 55^\circ
 \end{aligned}$$

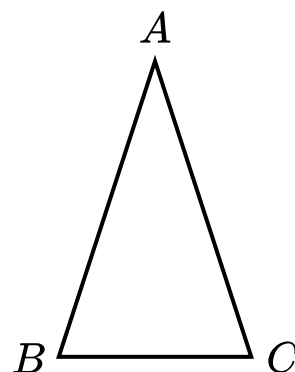


- ★ The perimeter of an isosceles triangle is 26 cm. The length of each equal side of the triangle is 10 cm long. The length of its base side is 6 cm.

$$26 - 10 \times 2 = 6 \text{ (cm)}$$

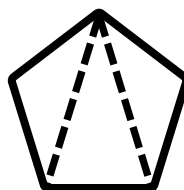
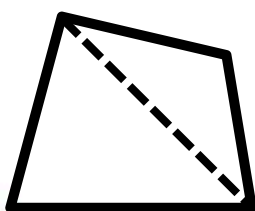
- ★ Given that  $AB = AC$  and  $m\angle B = 2m\angle A$ ,  $m\angle C =$  72  $^\circ$ .

$$\begin{aligned}
 m\angle A + m\angle B + m\angle C &= 180^\circ, m\angle B = m\angle C \\
 m\angle A + 2m\angle A + 2m\angle A &= 180^\circ \\
 5m\angle A &= 180^\circ \\
 m\angle A &= 36^\circ \\
 m\angle C &= 2m\angle A = 72^\circ
 \end{aligned}$$



## Challenge

- ★ We have learned that the sum of the interior angles of a triangle is  $180^\circ$ .  
 By dividing a quadrilateral into 2 triangles, we can find that the sum of its interior angles is  $180^\circ \times 2 = 360^\circ$ .  
 By dividing a pentagon into 3 triangles, we can find that the sum of its interior angles is  $180^\circ \times 3 = 540^\circ$ .  
 By dividing a hexagon into 4 triangles, we can find that the sum of its interior angles is 720  $^\circ$ .  
 By dividing an  $n$ -sided polygon into  $n-2$  triangles, we can find that the sum of its interior angles is  $180(n-2)$   $^\circ$ .



PreA Teacher Jia Ming  
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